

R

4 2016, 20 2017, 15 2017

Musical notation for the first system, featuring a treble clef, a key signature of one flat, and a 4/4 time signature. The notation includes various note values, rests, and dynamic markings.

T

Musical notation for the second system, featuring a treble clef, a key signature of one flat, and a 4/4 time signature. The notation includes various note values, rests, and dynamic markings.

Large calderas with areas of 100 km<sup>2</sup> or more are among the



dimensions and process timescales, and supports our hypothesis that bulk deformation at volcanoes can be approximated to that of a crust with a large and distributed population of small discontinuities.

The combined corrected uplift at Campi Flegrei (with intervals of stasis removed) also follows the classic elastic-brittle sequence for deformation in extension (Fig. 5). The crust behaves elastically for  $h < 1.75$  m and, after a short transition, becomes quasi-elastic for  $h > 2.3$  m with  $l_{ch} \approx 1$  m (Fig. 5). The current corrected uplift of about 4.2 m gives  $h/l_{ch} \approx 4.2$ , which suggests that the crust is now approaching the transition from quasi-elastic to inelastic deformation (Fig. 5). Virtually the same VT-uplift trend appears when using uplift uncorrected for secular subsidence (Fig. 5). Background subsidence since 1950 has not had a significant effect on events differential stress accumulation in the shallow crust.

The VT-uplift trend is similar to that observed at Rabaul and supports our view that the entire sequence of unrest since 1950 reflects a long-term accumulation of stress in the crust (Fig. 5). This interpretation is reinforced by the remaining interval of significant VT seismicity between 1972 and 1982 (Fig. 2), which was characterized by a gradual decay in VT event rate from 200 to

300 events per month and a minor corrected, ground subsidence and recovery of about 5% of the total uplift. This was followed by a new 30-month episode of corrected uplift that, for its first 8 months until March 1983, raised the ground at Pozzuoli by 0.4 m without significant seismicity. When VT events again occurred, they accelerated to rates of about 300–500 events per month in  $< 3$  months (Fig. 2).

The VT decay with minor ground movement resembles an extended aftershock sequence, in which fracturing and fault slip relax stresses in the surrounding rock under a constant bulk strain<sup>34</sup>. Before faulting can resume, the surrounding rock must be re-stressed elastically until the local stresses have returned to their values before relaxation<sup>35</sup>. Renewed uplift will thus occur without VT events until the stress necessary for continued faulting has been regained. From equation (1) the mean VT event rate  $dN/dt \approx [d(h)/dt][dN/d(h)] \approx [d(h)/dt][\Sigma N/h_{ch}]$ . If the same seismic sequence is maintained across uplifts, the final VT event rate in 1972 and the starting rate in 1982 will be characterized by the same value of  $\Sigma N/h_{ch}$ . Hence, the ratio of their respective event rates should be similar to the corresponding ratio of their mean rates of uplift. Such similarity is indeed observed: the ratio of VT event rates lies in the range  $0.7 \pm 0.3$ , which embraces the uplift-rate ratio of 0.8 for mean uplift rates of 0.57 m per year in 1969–1972 and 0.72 m per year in 1982–1984.

The increase in differential stress during elastic recovery is proportional to the accompanying uplift; it is also numerically equivalent to the stress previously lost by seismic relaxation. To a first approximation, stress and uplift change in proportion when behaviour is quasi-elastic<sup>23</sup>, so that the fraction of total stress lost during relaxation is approximately the ratio of uplift during elastic recovery to total uplift before relaxation, that is 0.4 out of 2.5 m or 16%. This value is consistent with independent estimates of the proportion of energy lost by seismicity during 1972–1982. The proportion of total stress relaxed by seismicity is  $\sim (E_s/E_T)^{1/2}$ , where  $E_s$  and  $E_T$  are the seismic energy released and total energy supplied<sup>36</sup>. Extrapolating the analysis of the 1982–1984 unrest<sup>19,20</sup>, the seismic energy lost during 1972–1982 is  $\sim 10^{13}$  J, where  $E_s$  is the total energy supplied until release  $E_{10} \approx F_{10} \Delta h / B$

additional increase in  $h$  by c. 1.8m. The corresponding

suggests that long-term stress accumulation may be a general feature of unrest at large calderas.

contribute to deformation (to permit greater uplift than from elastic-brittle behaviour); that additional intervals of fault slip

## Discussion

Our interpretation predicts that if the current uplift continues to a corrected value of about 4.5 m at Pozzuoli, the crust in Campi Flegrei will have returned to the stress conditions that prevailed in 1984 at the end of the last major uplift (Fig. 6). We would then expect any additional uplift to continue the VT-deformation trend interrupted in 1984 and, hence, to be accompanied by a significant increase in VT seismicity, regardless of the specific mechanism that is increasing the applied differential stress. Should the rate of uplift also return to the rapid values of 1982–1984, we would further expect the onset of VT event rates as high as 800–1,000 per month. Rapid uplift, however, is not essential. At Rabaul, for example, the approach to eruption was preceded by 2 years at a maximum recorded uplift rate of about 0.15 m per year, which was about three times smaller than the peak rates that had been registered 10 years previously<sup>24</sup>. A return to the long-term VT-deformation trend at Campi Flegrei may thus occur at uplift rates and VT event rates slower than observed during previous emergencies.

The indirect stress ratio  $h/l_{ch}$  suggests that the differential stress accumulated in Campi Flegrei's crust is about four times its tensile strength (Fig. 5) and so is approaching the transition from quasi-elastic to inelastic deformation regimes. An increase in linkage among small-scale cracks between faults is also expected to occur at the transition to inelastic behaviour. This would favour an increase in bulk permeability and, hence, a faster escape of fluids from the geothermal system, which is consistent with the onset of corrected subsidence in 1984. A return to the long-term VT-deformation trend may therefore be characterized by inelastic behaviour under a constant maintained stress, for which increases in total deformation are determined by additional fault movement (Fig. 3). Such a transition would be associated with VT event rates increasing in proportion to the rate of uplift.

The few field data available for large calderas and stratovolcanoes suggest that the quasi-elastic regime contributes between 40 and 80% of the total precursory deformation (Fig. 4). Assuming this range, a corrected uplift of 4.2 m at the end of quasi-elastic behaviour at Campi Flegrei (Fig. 5) indicates that the inelastic regime may continue until reaching a total corrected uplift of between 5 and 10 m before an eruption can be expected. A transitional value of 4 for  $h/l_{ch}$  assumes that bulk failure occurs in tension. The value increases towards 5.6 as the failure mechanism involves tension with an increasing component of shear<sup>27–29</sup>. Increasing shear could thus raise the transitional uplift by some 25% and, hence, yield a total corrected uplift of between 6.25 and 12.5 m before an eruption.

The estimated limits on total uplift are smaller than the 17 m of caldera-wide uplift inferred to have occurred during the century before the caldera's last eruption in 1538 (refs 2,6). A greater total uplift would be favoured by a larger uplift before the transition to inelastic behaviour, without necessarily changing the proportion of uplift in the two deformation regimes, or by a greater proportion of uplift in the inelastic regime alone. A larger transitional uplift would be favoured if the pre-1538 intrusions had been required to break connected horizons of rock stronger than those providing resistance today (to increase the uplift required before tensile failure). Otherwise, the difference may indicate that mechanisms for reducing effective bulk rigidity, such as bedding-plane slip<sup>43,44</sup>, become significant as deformation proceeds (to enable greater uplift for a given applied stress); that, at timescales of  $\sim 10^2$  years, non-brittle (and seismically quiet) processes, such as viscous flow<sup>19</sup>, also



